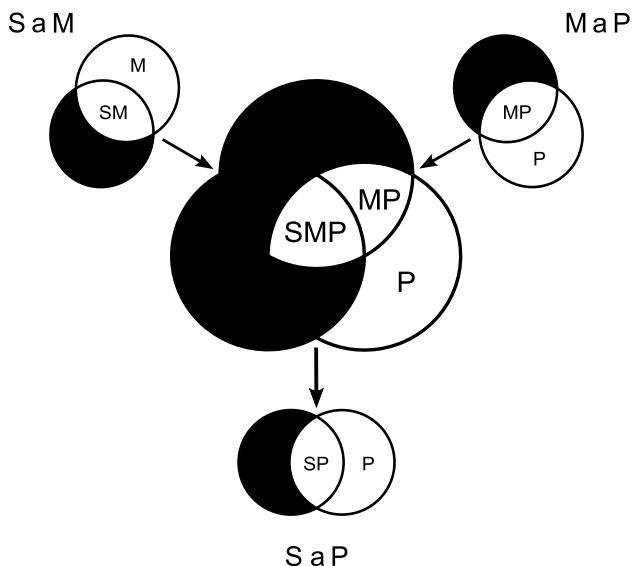
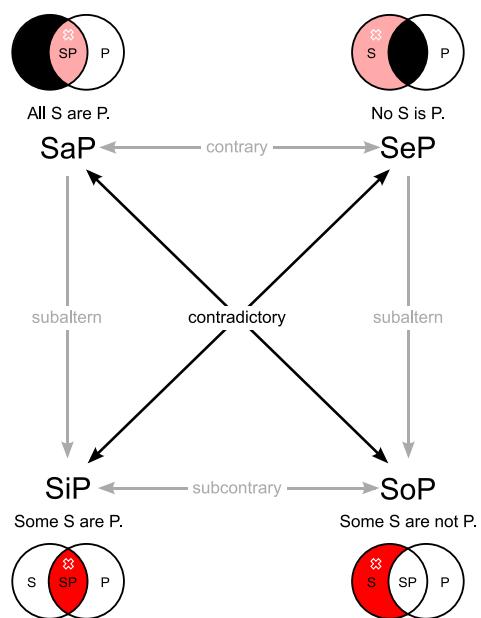


AAA-1 Modus Barbara

$\exists x: Mx \wedge \neg Px$	M a P	All M are P,
$\wedge \exists x: Sx \wedge \neg Mx$	S a M	and all S are M;
$\Rightarrow \exists x: Sx \wedge \neg Px$	S a P	thus all S are P.

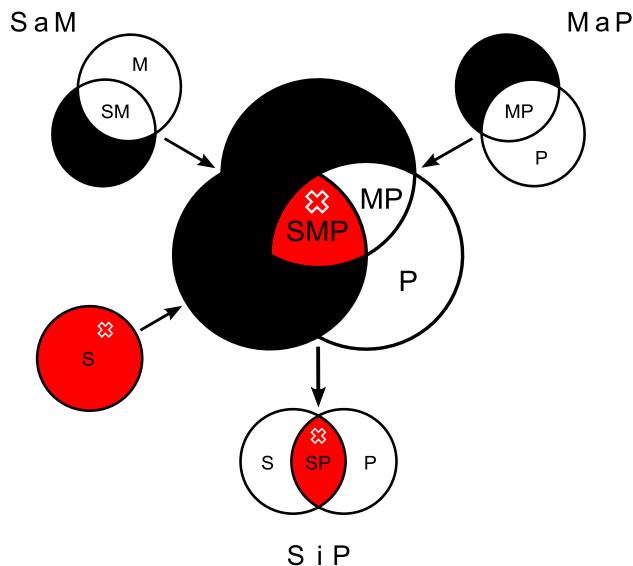


Square of opposition:



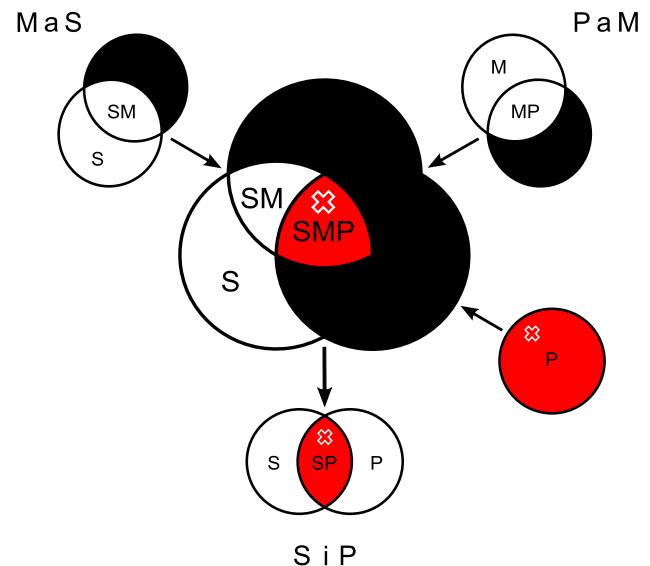
AAI-1 Modus Barbari

$\exists x: Mx \wedge \neg Px$	M a P	All M are P,
$\wedge \exists x: Sx \wedge \neg Mx$	S a M	and all S are M,
$\wedge \exists x: Sx$		and some S exist;
$\Rightarrow \exists x: Sx \wedge \neg Px$	S i P	thus some S are P.



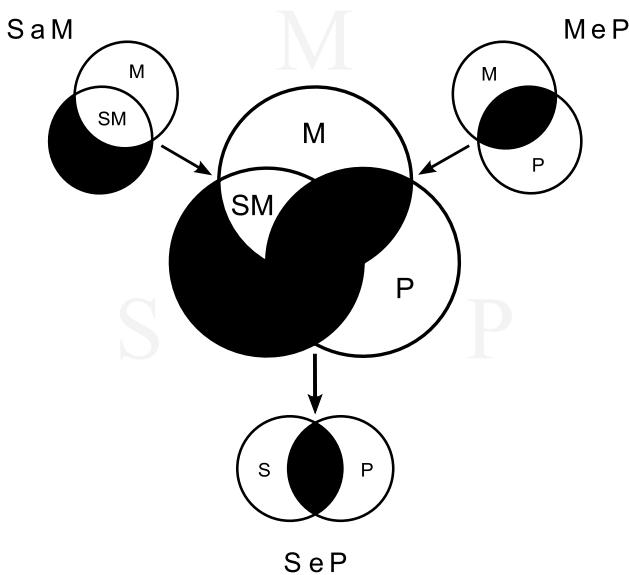
AAI-4 Modus Bamalip

$\exists x: Px \wedge \neg Mx$	P a M	All P are M,
$\wedge \exists x: Mx \wedge \neg Sx$	Ma S	and all M are S,
$\wedge \exists x: Px$		and some P exist;
$\Rightarrow \exists x: Sx \wedge \neg Px$	S i P	thus some S are P.



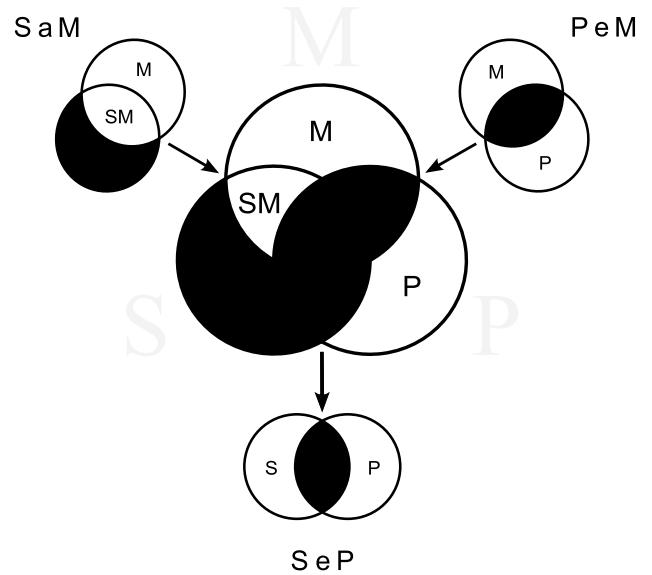
EAE-1 Modus Celarent

$\frac{\exists x: Mx \wedge Px}{\wedge \exists x: Sx \wedge \overline{Mx}}$ $M e P$ No M is P,
 $\Rightarrow \exists x: Sx \wedge Px$ $S a M$ and all S are M;
 $S e P$ thus no S is P.



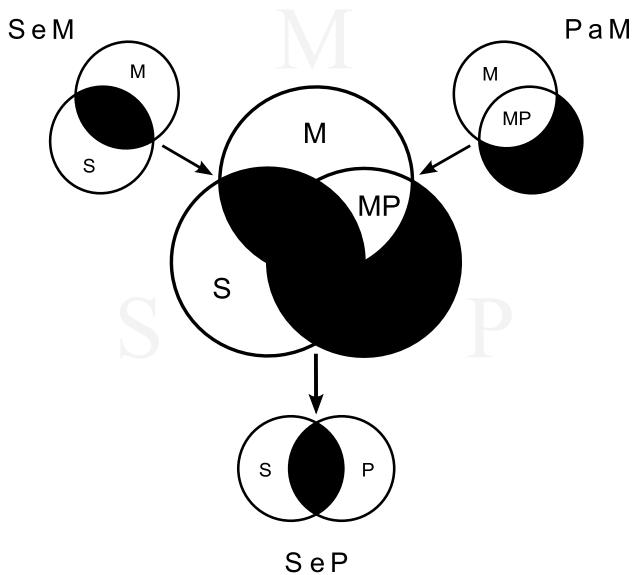
EAE-2 Modus Cesare

$\frac{\exists x: Px \wedge \overline{Mx}}{\wedge \exists x: Sx \wedge \overline{Mx}}$ $P e M$ No P is M,
 $\Rightarrow \exists x: Sx \wedge Px$ $S a M$ and all S are M;
 $S e P$ thus no S is P.



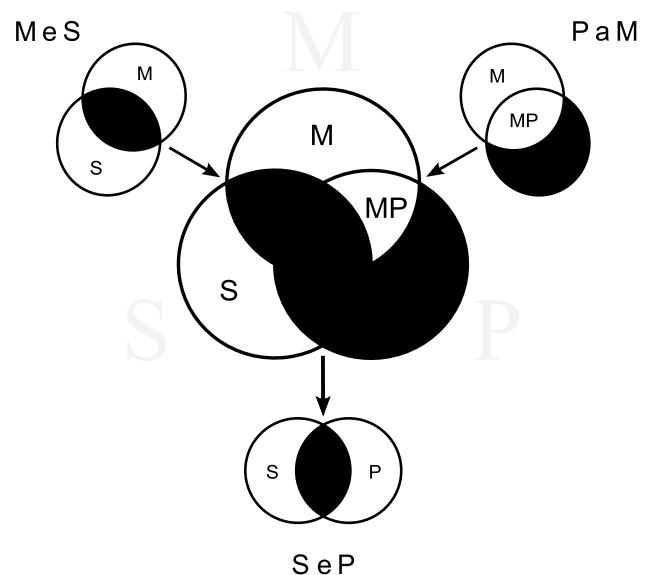
AEE-2 Modus Camestres

$\frac{\exists x: Px \wedge \overline{Mx}}{\wedge \exists x: Sx \wedge Mx}$ $P a M$ All P are M,
 $\Rightarrow \exists x: Sx \wedge Px$ $S e M$ and no S is M;
 $S e P$ thus no S is P.



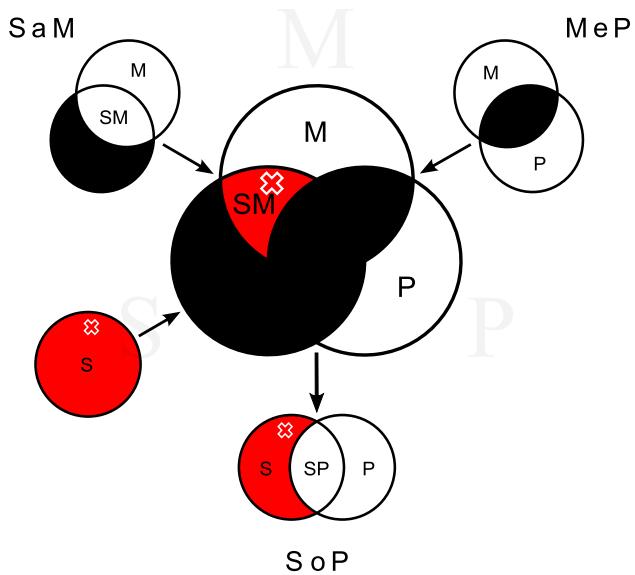
AEE-4 Modus Calemes

$\frac{\exists x: Px \wedge \overline{Mx}}{\wedge \exists x: Mx \wedge Sx}$ $P a M$ All P are M,
 $\Rightarrow \exists x: Sx \wedge Px$ $M e S$ and no M is S;
 $S e P$ thus no S is P.



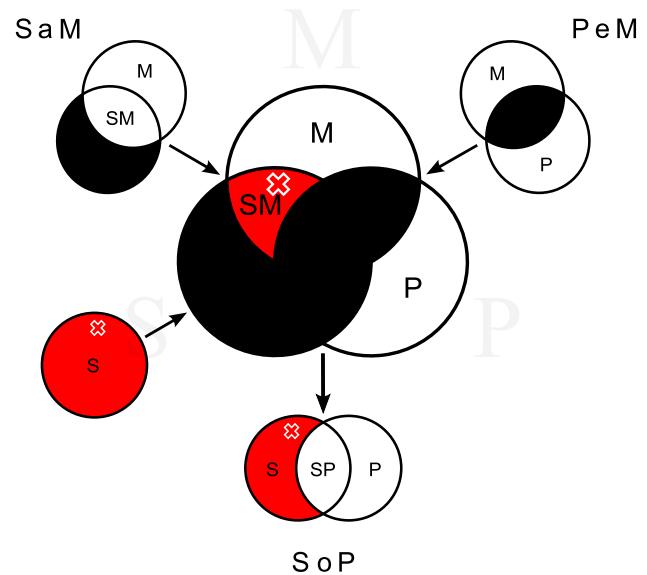
EAO-1 Modus Celaront

$\exists x: Mx \wedge Px$	M e P	No M is P,
$\wedge \exists x: Sx \wedge \overline{Mx}$	S a M	and all S are M,
$\wedge \exists x: Sx$		and some S exist;
$\Rightarrow \exists x: Sx \wedge \overline{Px}$	S o P	thus some S are not P.



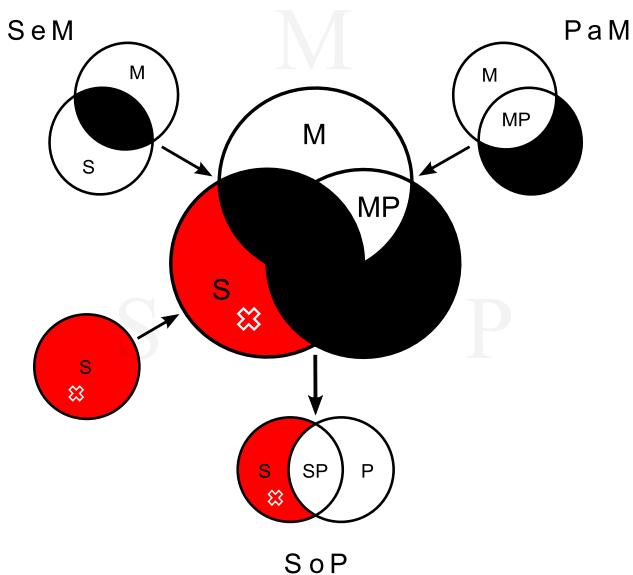
EAO-2 Modus Cesaro

$\exists x: Px \wedge \overline{Mx}$	P e M	No P is M,
$\wedge \exists x: Sx \wedge \overline{Mx}$	S a M	and all S are M,
$\wedge \exists x: Sx$		and some S exist;
$\Rightarrow \exists x: Sx \wedge \overline{Px}$	S o P	thus some S are not P.



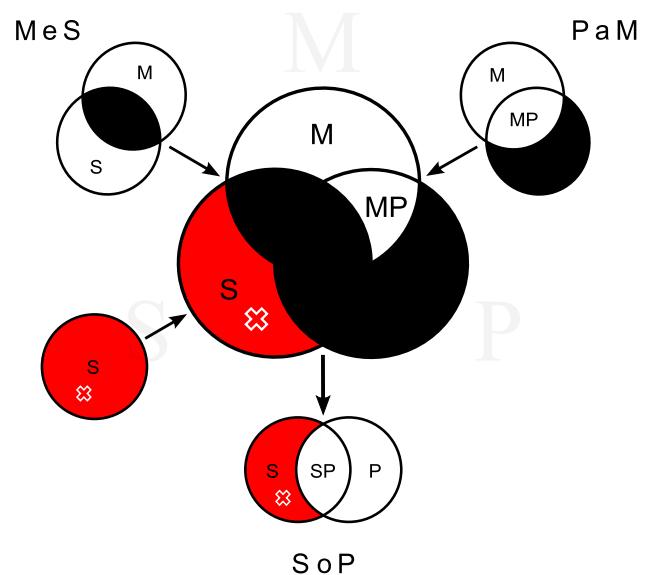
AEO-2 Modus Camestros

$\exists x: Px \wedge \overline{Mx}$	P a M	All P are M,
$\wedge \exists x: Sx \wedge \overline{Mx}$	S e M	and no S is M,
$\wedge \exists x: Sx$		and some S exist;
$\Rightarrow \exists x: Sx \wedge \overline{Px}$	S o P	thus some S are not P.



AEO-4 Modus Calemos

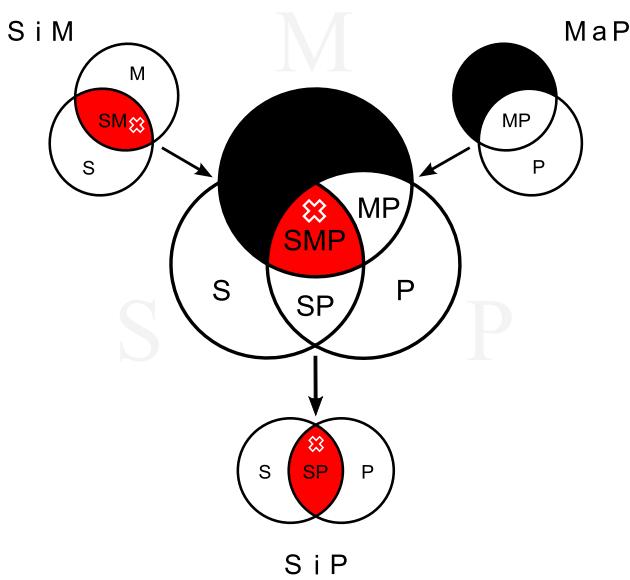
$\exists x: Px \wedge \overline{Mx}$	P a M	All P are M,
$\wedge \exists x: Mx \wedge \overline{Sx}$	M e S	and no M is S;
$\wedge \exists x: Sx$		and some S exist;
$\Rightarrow \exists x: Sx \wedge \overline{Px}$	S o P	thus some S are not P.



All-1 Modus Darii

$\exists x: Mx \wedge Px$ MaP
 $\wedge \exists x: Sx \wedge Mx$ SiM
 $\Rightarrow \exists x: Sx \wedge Px$ SiP

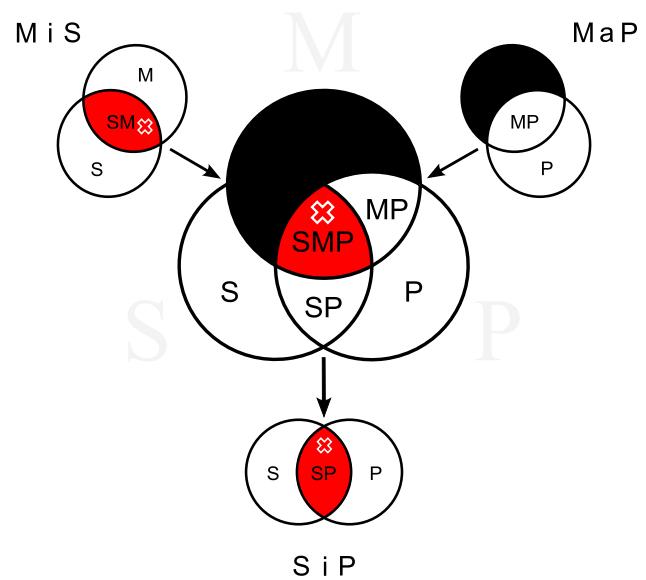
All M are P,
and some S are M;
thus some S are P.



All-3 Modus Datisi

$\exists x: Mx \wedge Px$ MaP
 $\wedge \exists x: Mx \wedge Sx$ MiS
 $\Rightarrow \exists x: Sx \wedge Px$ SiP

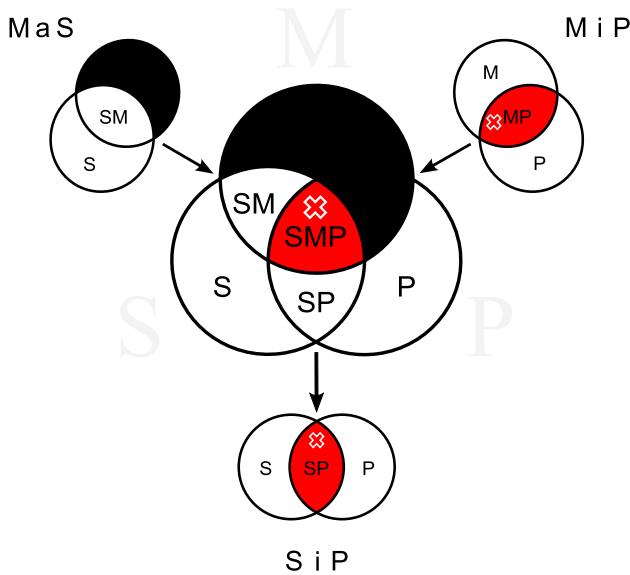
All M are P,
and some M are S;
thus some S are P.



IAI-3 Modus Disamis

$\exists x: Mx \wedge Px$ MiP
 $\wedge \exists x: Mx \wedge Sx$ MaS
 $\Rightarrow \exists x: Sx \wedge Px$ SiP

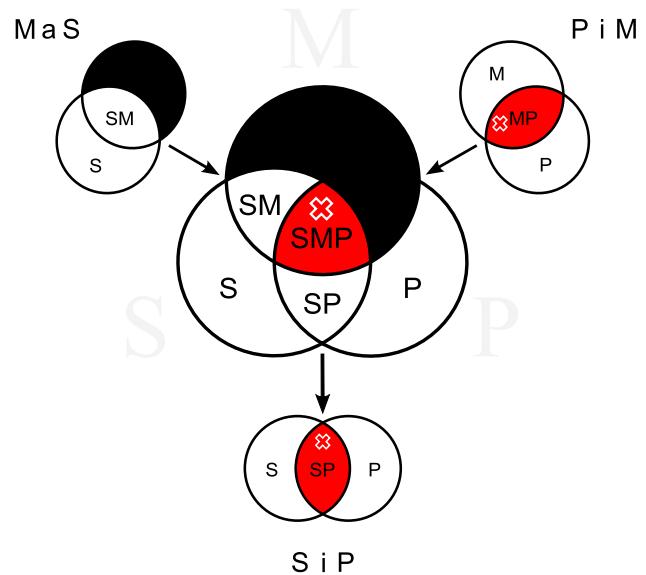
Some M are P,
and all M are S;
thus some S are P.



IAI-4 Modus Dimatis

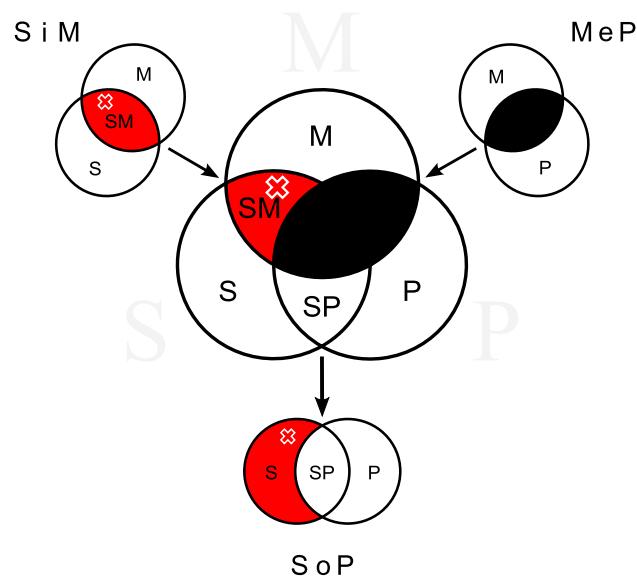
$\exists x: Px \wedge Mx$ PiM
 $\wedge \exists x: Mx \wedge Sx$ MaS
 $\Rightarrow \exists x: Sx \wedge Px$ SiP

Some P are M,
and all M are S;
thus some S are P.



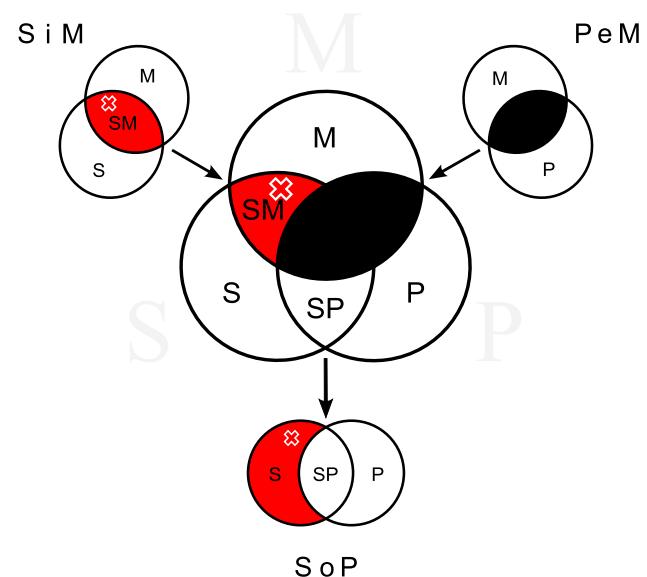
EIO-1 Modus Ferio

$\exists x: Mx \wedge Px$ $M e P$ No M is P ,
 $\wedge \exists x: Sx \wedge Mx$ $S i M$ and some S are M ;
 $\Rightarrow \exists x: Sx \wedge \overline{Px}$ $S o P$ thus some S are not P .



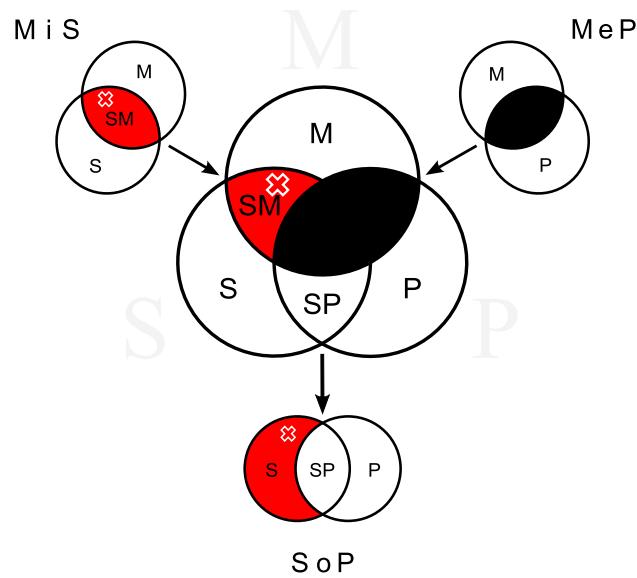
EIO-2 Modus Festino

$\exists x: Px \wedge Mx$ $P e M$ No P is M ,
 $\wedge \exists x: Sx \wedge Mx$ $S i M$ and some S are M ;
 $\Rightarrow \exists x: Sx \wedge \overline{Px}$ $S o P$ thus some S are not P .



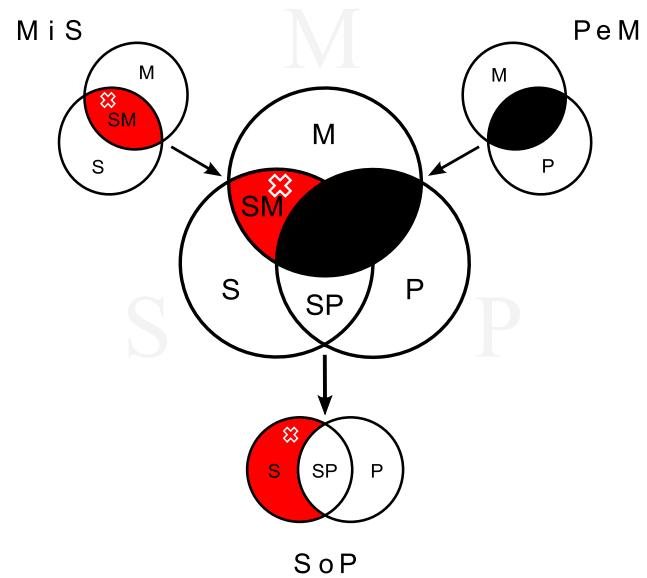
EIO-3 Modus Ferison

$\exists x: Mx \wedge \overline{Px}$ $M e P$ No M is P ,
 $\wedge \exists x: Mx \wedge Sx$ $M i S$ and some M are S ;
 $\Rightarrow \exists x: Sx \wedge \overline{Px}$ $S o P$ thus some S are not P .



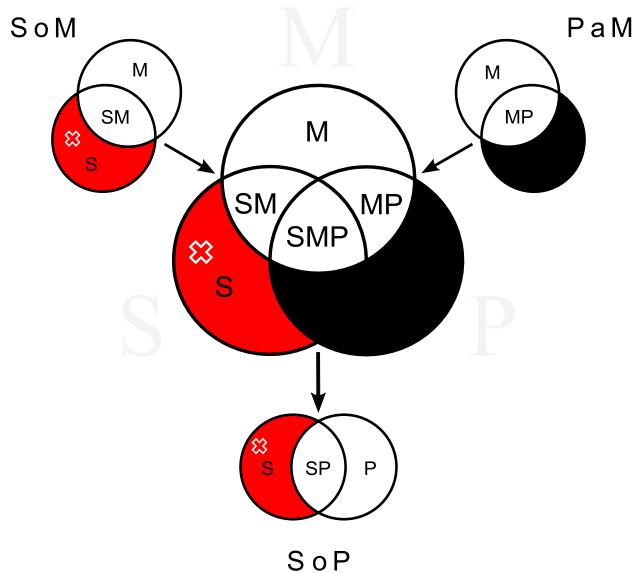
EIO-4 Modus Fresison

$\exists x: Px \wedge Mx$ $P e M$ No P is M ,
 $\wedge \exists x: Mx \wedge Sx$ $M i S$ and some M are S ;
 $\Rightarrow \exists x: Sx \wedge \overline{Px}$ $S o P$ thus some S are not P .



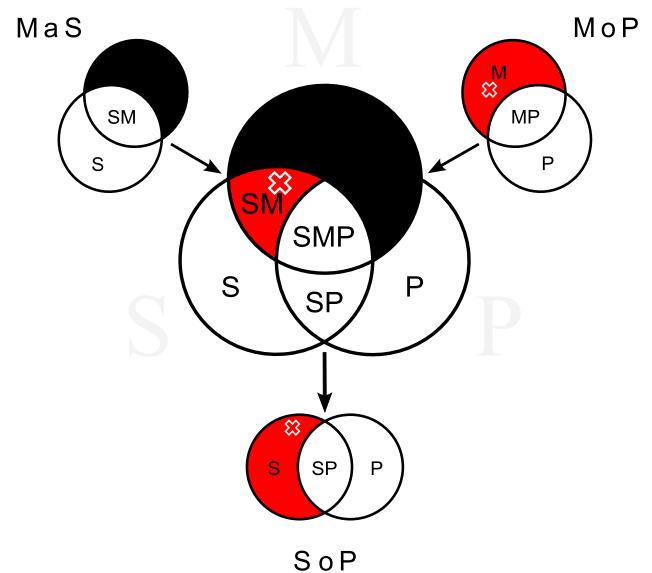
AOO-2 Modus Baroco

$\exists x: P \times \overline{M} \times$	P a M	All P are M,
$\wedge \exists x: S \times \overline{M} \times$	S o M	and some S are not M;
$\Rightarrow \exists x: S \times \overline{P} \times$	S o P	thus some S are not P.



OAO-3 Modus Bocardo

$\exists x: M \times \overline{P} \times$	M o P	Some M are not P,
$\wedge \exists x: M \times S \times$	M a S	and all M are S;
$\Rightarrow \exists x: S \times \overline{P} \times$	S o P	thus some S are not P.

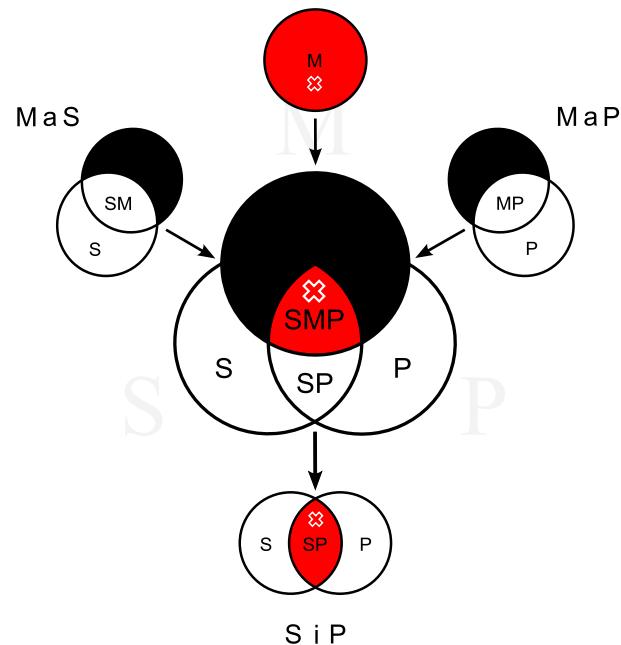


Venn diagrams are easily transformed into Euler diagrams:



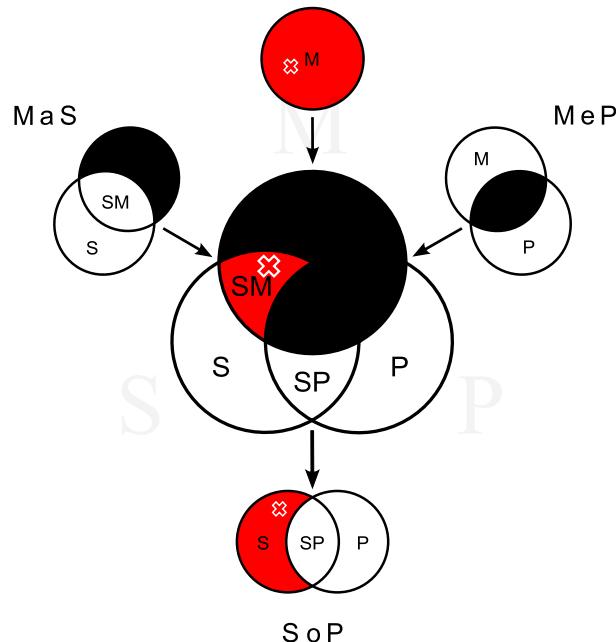
AAI-3 Modus Darapti

$\exists x: Mx \wedge \overline{Px}$	M a P	All M are P,
$\wedge \exists x: Mx \wedge \overline{Sx}$	M a S	and all M are S,
$\wedge \exists x: Mx$		and some M exist;
$\Rightarrow \exists x: Sx \wedge Px$	S i P	thus some S are P.



EAO-3 Modus Felapton

$\exists x: Mx \wedge Px$	M e P	No M is P,
$\wedge \exists x: Mx \wedge \overline{Sx}$	M a S	and all M are S,
$\wedge \exists x: Mx$		and some M exist;
$\Rightarrow \exists x: Sx \wedge \overline{Px}$	S o P	thus some S are not P.



EAO-4 Modus Fesapo

$\exists x: Px \wedge Mx$	P e M	No P is M,
$\wedge \exists x: Mx \wedge \overline{Sx}$	M a S	and all M are S,
$\wedge \exists x: Mx$		and some M exist;
$\Rightarrow \exists x: Sx \wedge \overline{Px}$	S o P	thus some S are not P.

